

Accurate Rydberg quantum simulations of spin-1/2 models

ICQSIM — Paris — November 16, 2017

Theory

Sebastian Weber, Hans Peter Büchler (*University of Stuttgart*)

Experiment

Sylvain De Léséleuc, Vincent Lienhard, Daniel Barredo, Thierry Lahaye, Antoine Browaeys (*Université Paris-Saclay*)

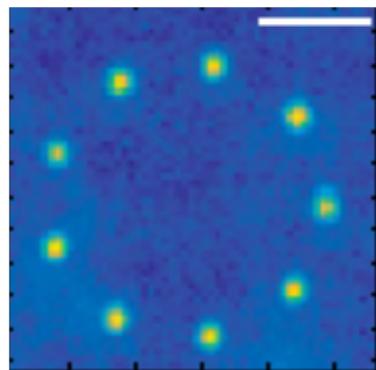
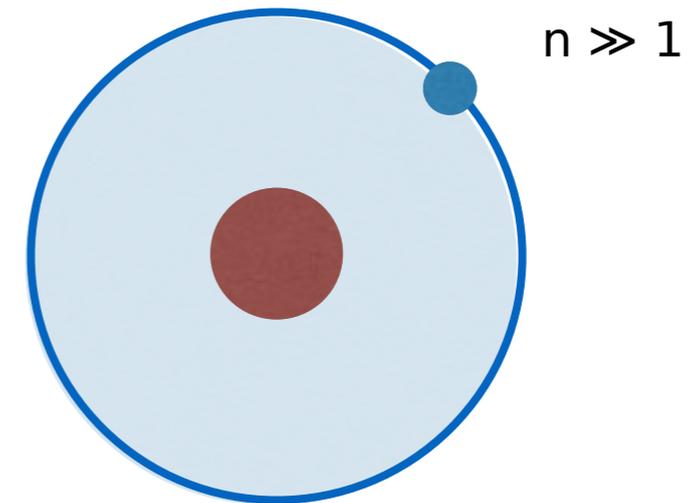
Rydberg quantum simulations of spin Hamiltonians

- **Strong interactions**

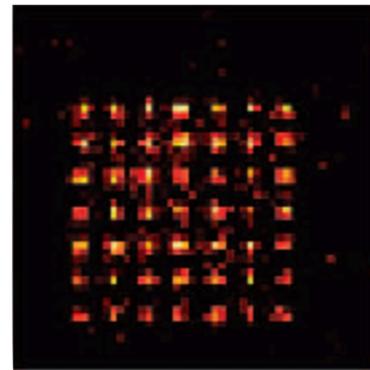
- I) dipole-dipole $\sim n^4/R^3$
- II) van der Waals $\sim n^{11}/R^6$, anisotropy possible
- III) cutoff potentials via Rydberg dressing

- **Long radiative lifetime $\sim n^3$**

- **Defect-free arbitrary atom arrays experimentally realized**



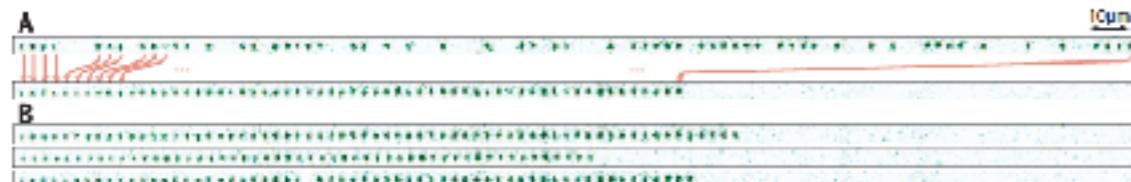
H. Kim et al.,
Nat. Commun. **7**,
13317 (2016)



D. Barredo et al.,
Science **354**,
6315 (2016)

Basis size for 49 spin-1/2 particles: $2^{49} \approx 6 \cdot 10^{14}$

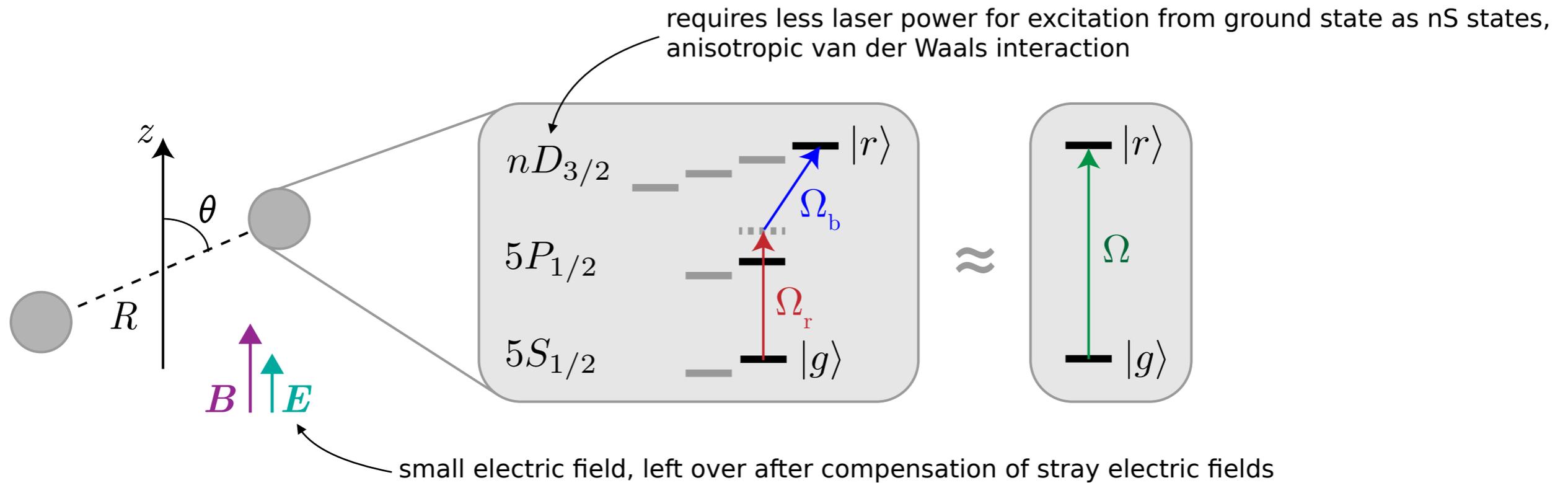
→ direct numerical simulations intractable



M. Endres et al.,
Science **354**,
6315 (2016)

- **Requirement: accurate mapping of multilevel Rydberg atoms to spins with just a few levels**

Example: Ising-like system of spin-1/2 particles



We want to map the Rydberg atoms to spin-1/2 particles:

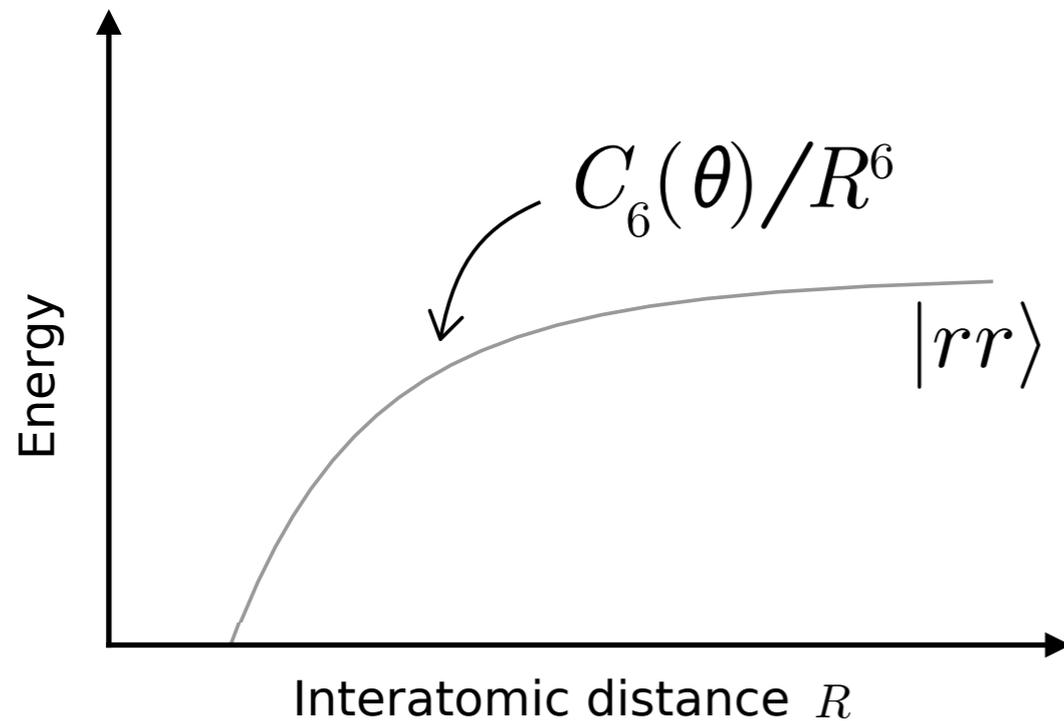
- $|g\rangle \rightarrow |\downarrow\rangle$, $|r\rangle \rightarrow |\uparrow\rangle$
- effective interaction between $|r\rangle_i$ and $|r\rangle_j$: U_{ij}

$$\rightarrow H = \sum_i \frac{\hbar\Omega}{2} \sigma_x^i + \frac{1}{2} \sum_{i \neq j} U_{ij} n_i n_j \quad \text{with } \sigma_x^i = |r\rangle \langle g|_i + |g\rangle \langle r|_i, \quad n_i = |r\rangle \langle r|_i$$

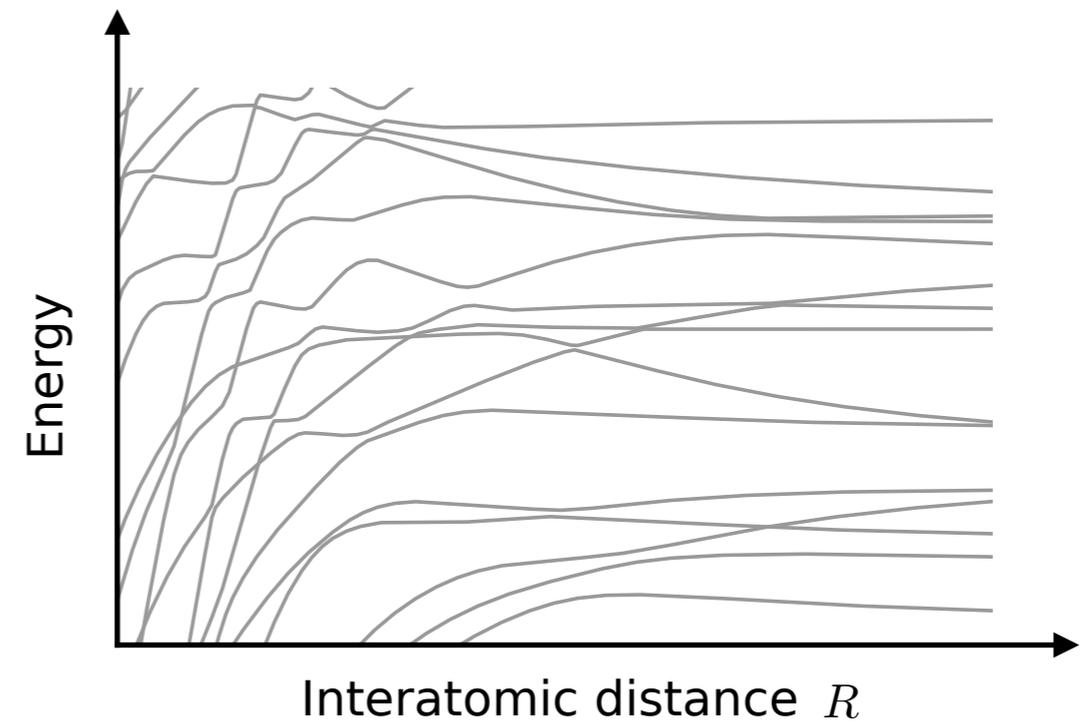
Ising-like model with transverse field

Example: Ising-like system of spin-1/2 particles

Ideal interaction potential



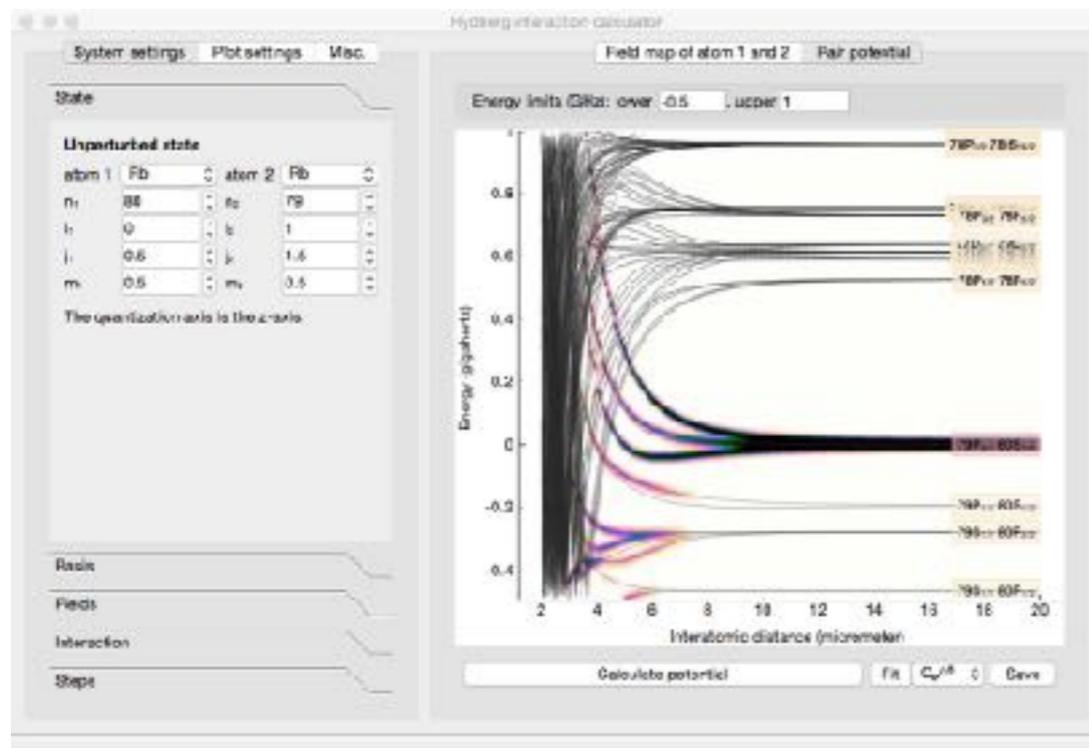
How reality looks like for generic experimental parameters



- Describing atoms as two-level systems is an approximation that can be difficult to fulfill
- Determination of suitable parameters requires calculation of Rydberg pair interaction potentials

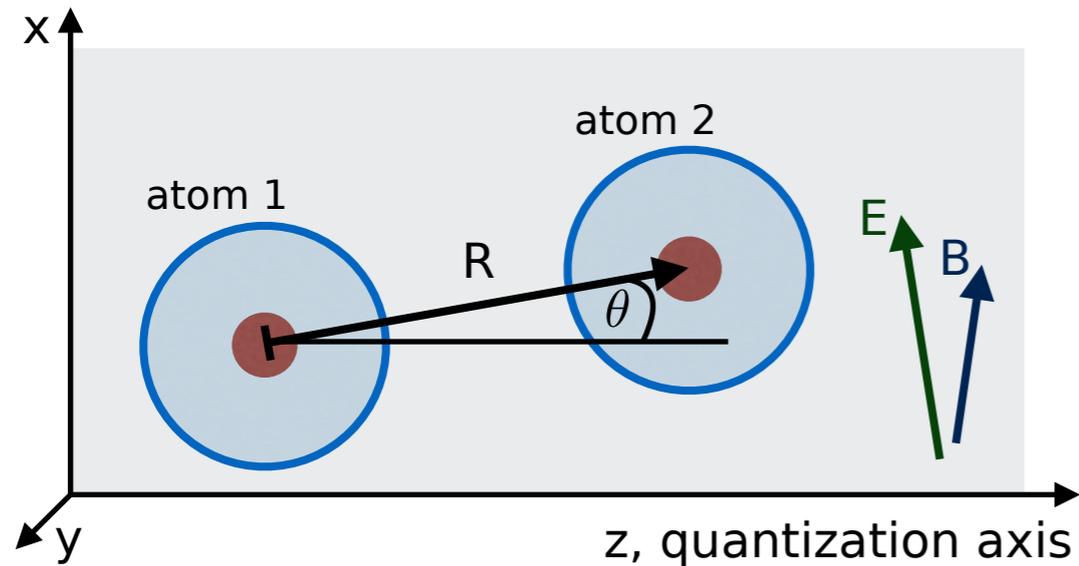
Non-perturbative calculation of Rydberg pair interaction potentials

J. Phys. B 50, 133001 (2017)



Pair potential calculation

Step 1: set up the Hamiltonian



- Born-Oppenheimer approximation
- $R >$ Le Roy radius
 - multipole approximation, no exchange interaction
- $R <$ wavelength of Rydberg-Rydberg transitions
 - no retardation effects

$$H = (H_{\text{atom1}} + H_{\text{atom1-fields}}) \otimes \mathbb{1} + \mathbb{1} \otimes (H_{\text{atom2}} + H_{\text{atom2-fields}}) + H_{\text{multipole interaction}}$$

energies of unperturbed Rydberg states

interaction with static E and B-fields

interaction between the two Rydberg atoms

Pair potential calculation

Step 2: define the basis

Full basis set:

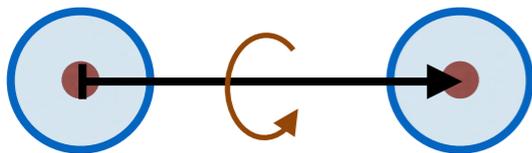
Set of all pair states $|n_1, l_1, j_1, m_{j1}\rangle \otimes |n_2, l_2, j_2, m_{j2}\rangle$

Restricted basis set:

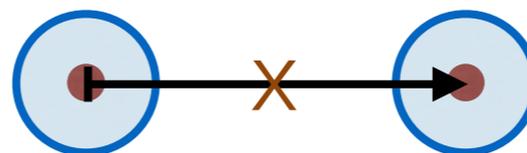
If interested in the pair potential of the pair state $|\psi\rangle$, restrict basis to states with ...

- similar *energy* as $|\psi\rangle$
- similar *principal and momentum quantum number* as $|\psi\rangle$
- same *symmetry* as $|\psi\rangle$

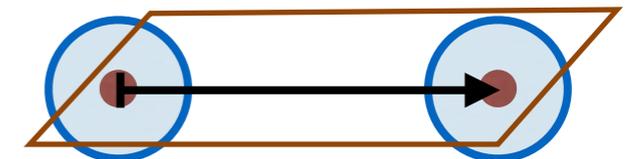
Rotation: $m_{j1} + m_{j2}$ conserved



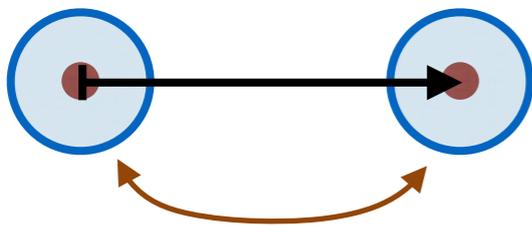
Inversion



Reflection



Permutation (if no interaction of higher order than dipole-dipole)



Pair potential calculation

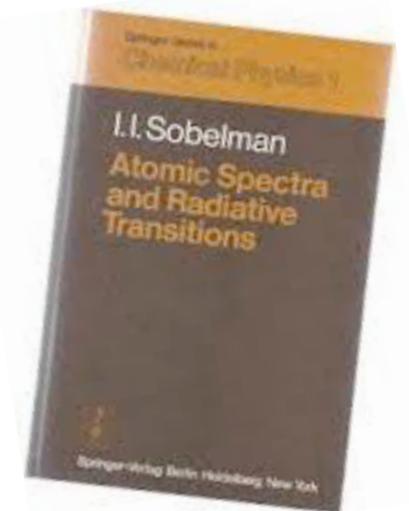
Step 3: diagonalize the Hamiltonian within the basis

$$\begin{pmatrix} \langle b_1 | H | b_1 \rangle & \langle b_1 | H | b_2 \rangle & \cdots \\ \langle b_2 | H | b_1 \rangle & \langle b_2 | H | b_2 \rangle & \cdots \\ \vdots & \vdots & \ddots \end{pmatrix}$$

where $|b_i\rangle$ are basis elements

Calculate matrix elements $\langle b_i | H | b_j \rangle$

- decompose into single atom matrix elements
- radial and angular part separate
 - radial matrix elements:
radial Schrödinger equation
 - angular matrix elements:
Wigner-Eckart theorem



Diagonalize the Hamiltonian matrix

→ eigen energies plotted as a function of the interatomic distance make up the pair potentials

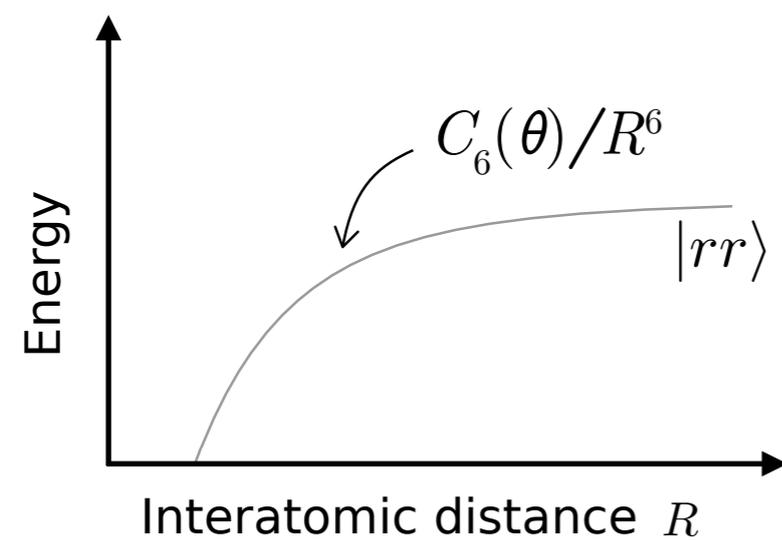
Our *Pairinteraction* software is available as open-source: <https://pairinteraction.github.io>

Similar open-source project by Nikola Šibalić et al.: <https://github.com/nikolasibalic/ARC-Alkali-Rydberg-Calculator>

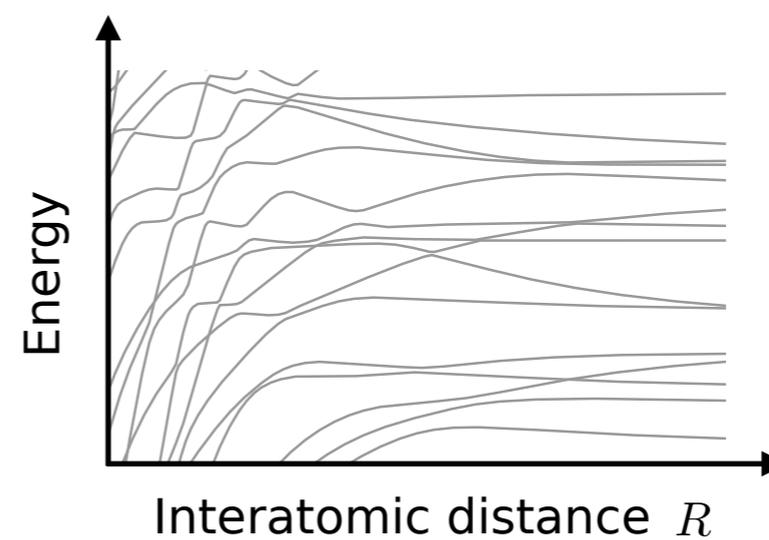
Usage of pair interaction potentials for the determination of optimal parameters

arXiv:1710.06156 (2017)

Ideal interaction potential

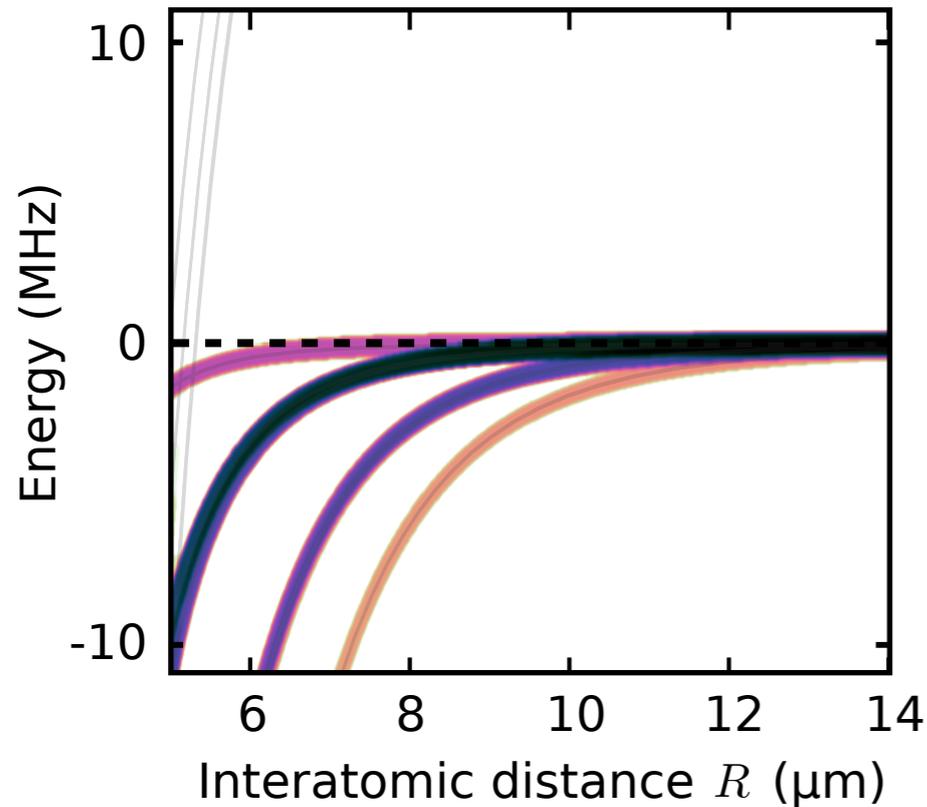


Reality for generic parameters



Influence of B-fields on pair potentials

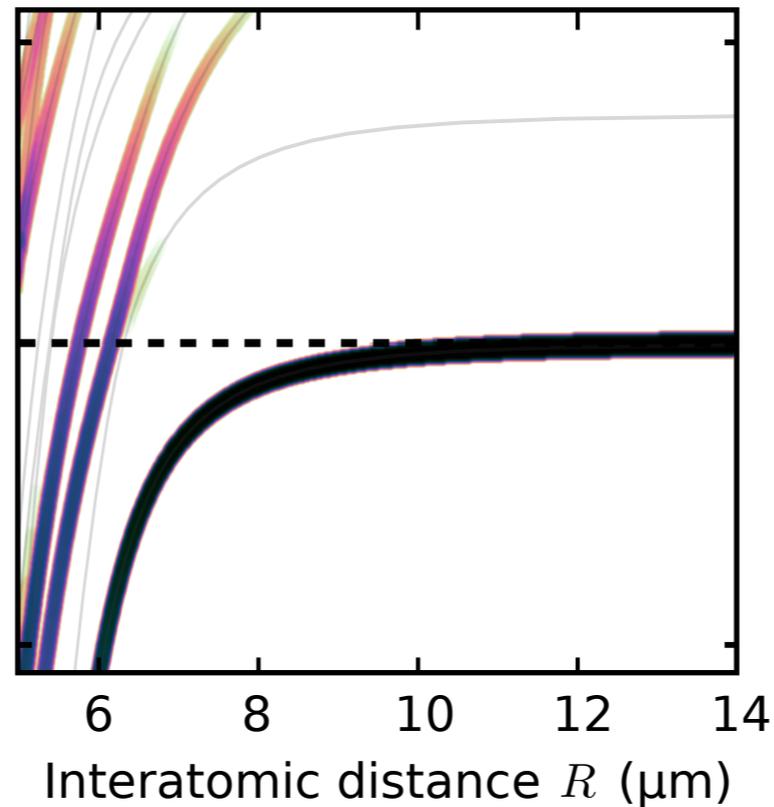
B = 0 G



Degenerate Zeeman levels

T. G. Walker and M. Saffman, Phys. Rev. A **77**, 032723 (2008)

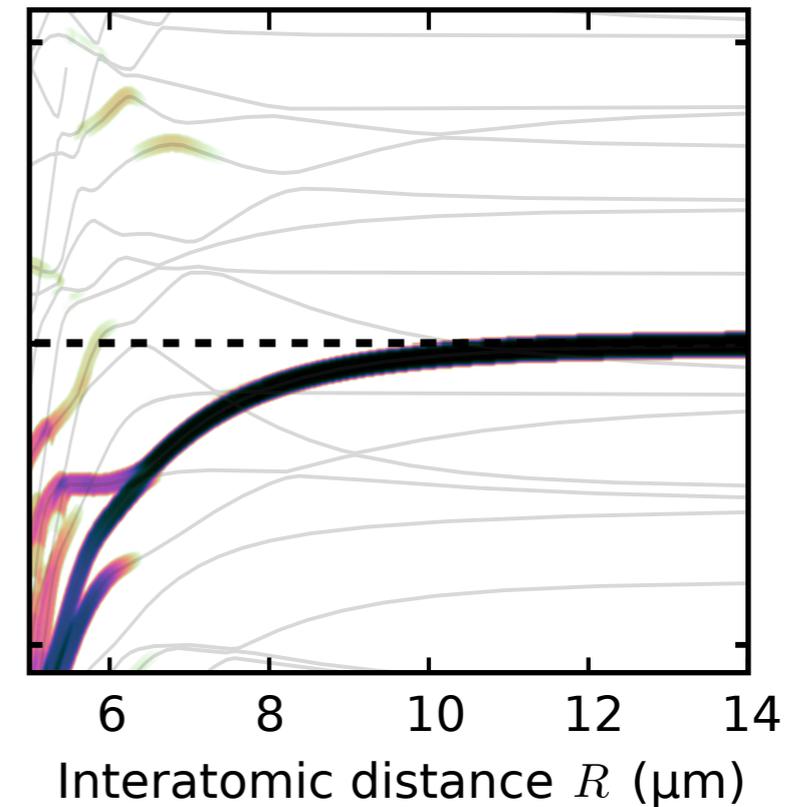
B = -6.9 G



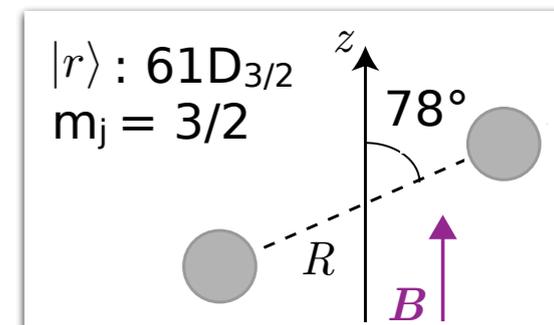
Crossing Zeeman levels

B. Vermersch et al., Phys. Rev. A **91**, 023411 (2015)

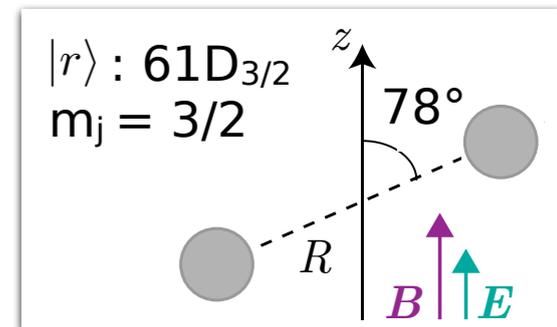
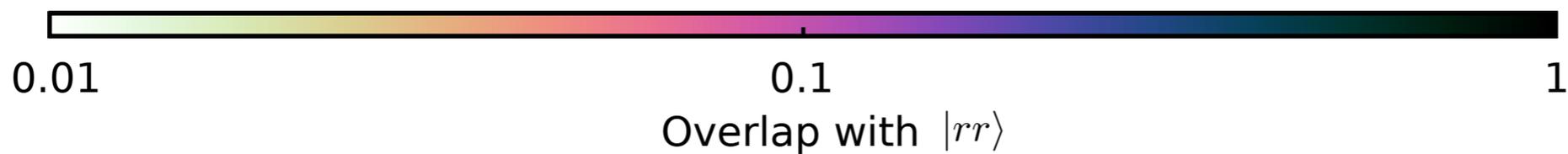
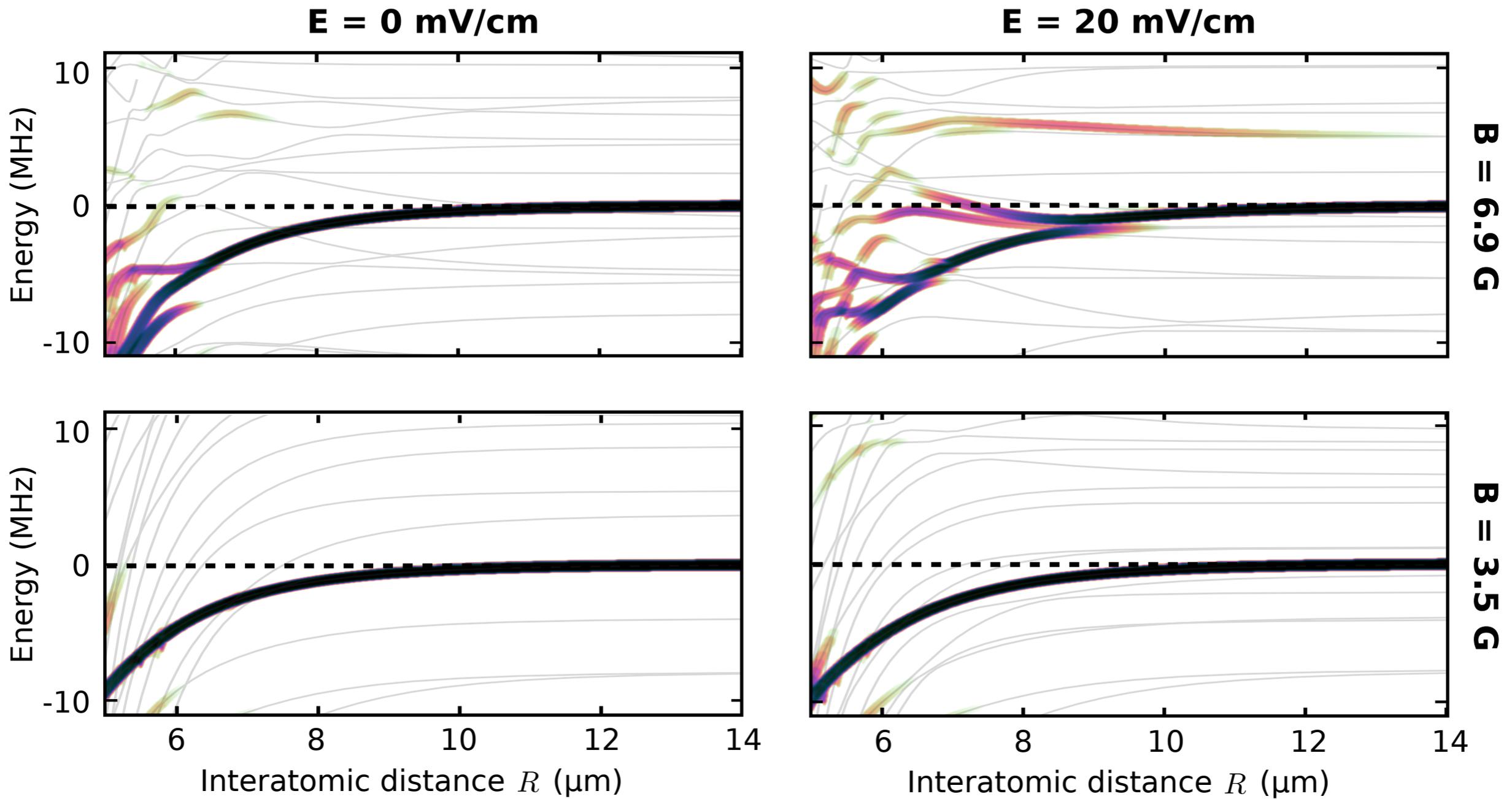
B = 6.9 G



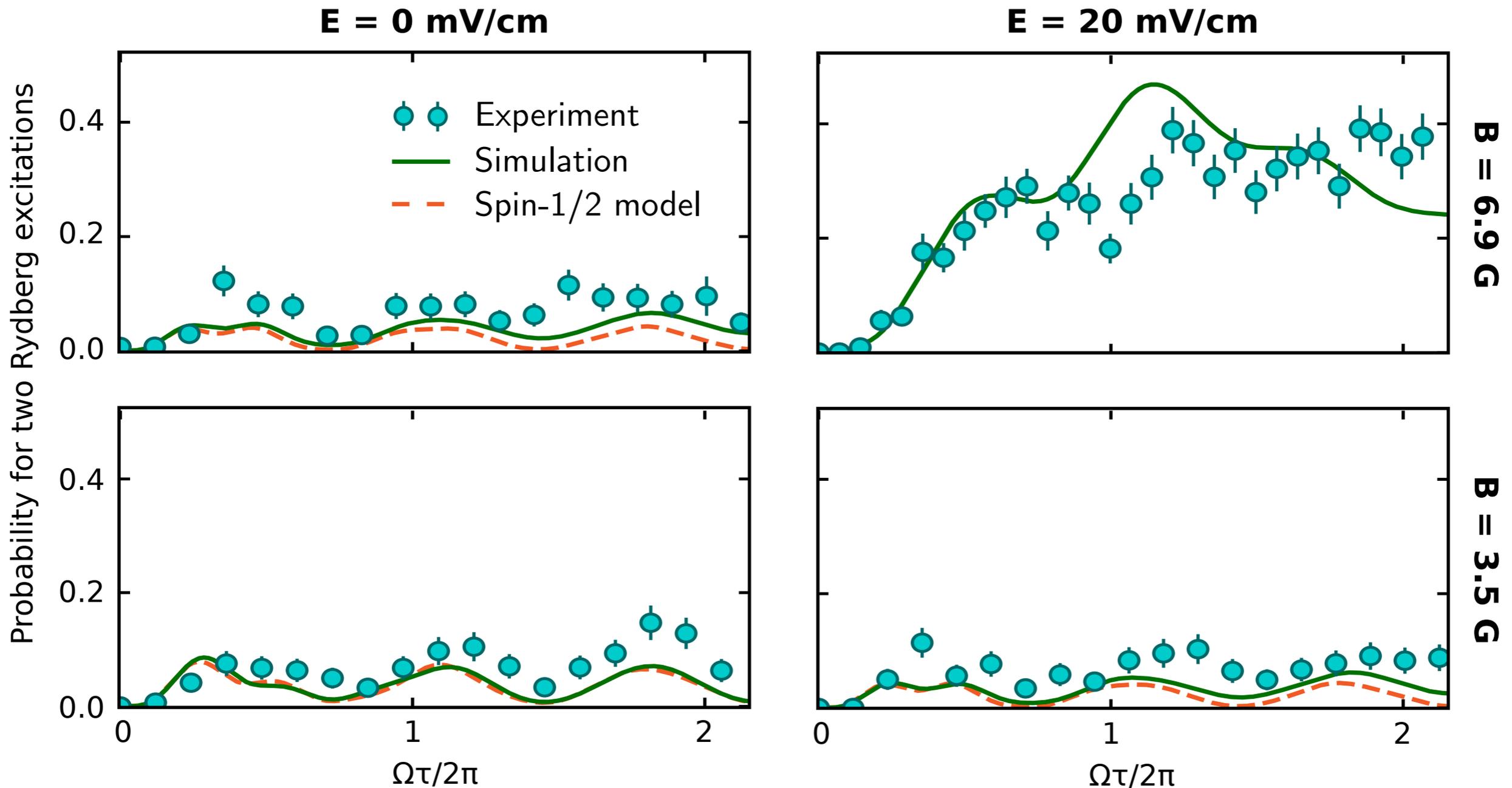
Reasonable Rydberg blockade



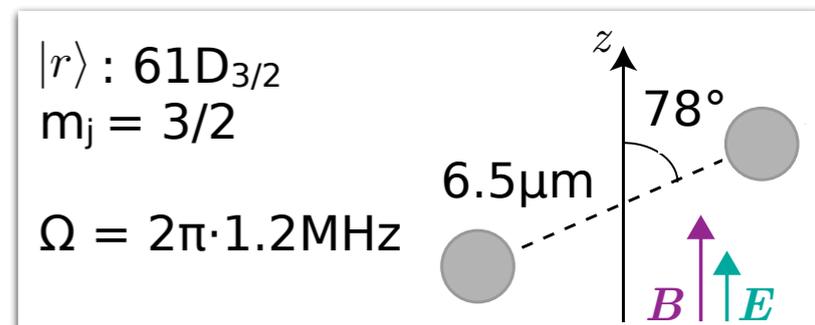
Influence of an additional small E-field



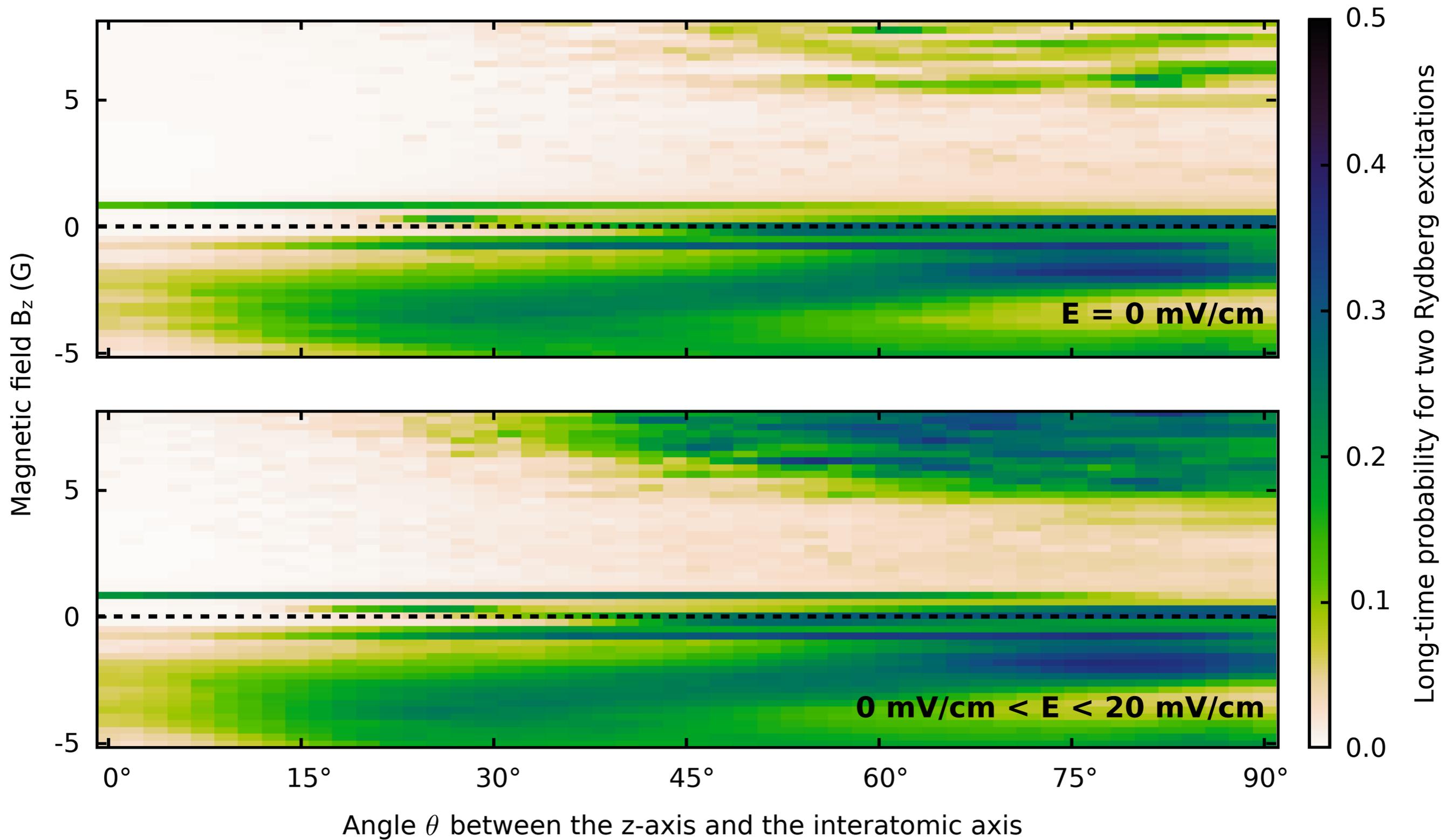
Experimental test of the predictions



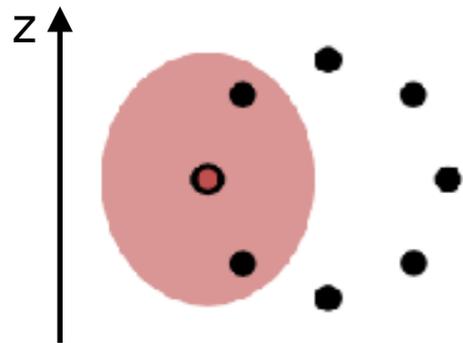
Predicted breakdown of Rydberg blockade experimentally seen as increasing probability for two Rydberg excitations



Influence of geometry

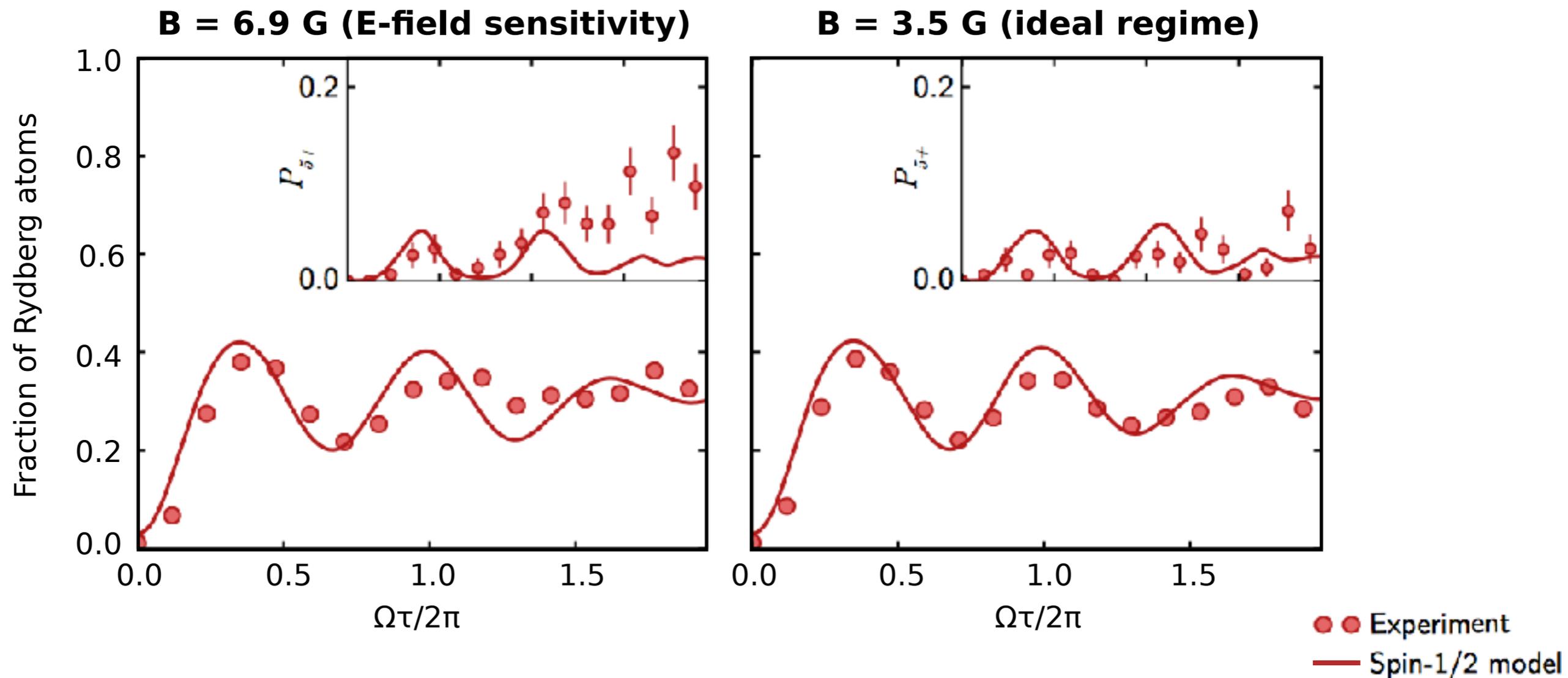


Quantum simulation of a 8-atom ring

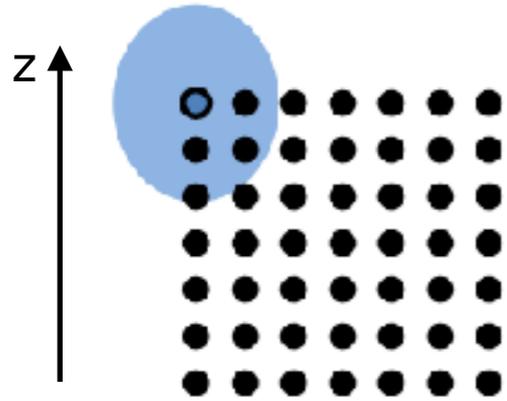


Prior to the experiment, stray electric field compensated better than 5 mV/cm

Revisit of the experiment reported in H. Labuhn et al., Nature **534**, 667 (2016)

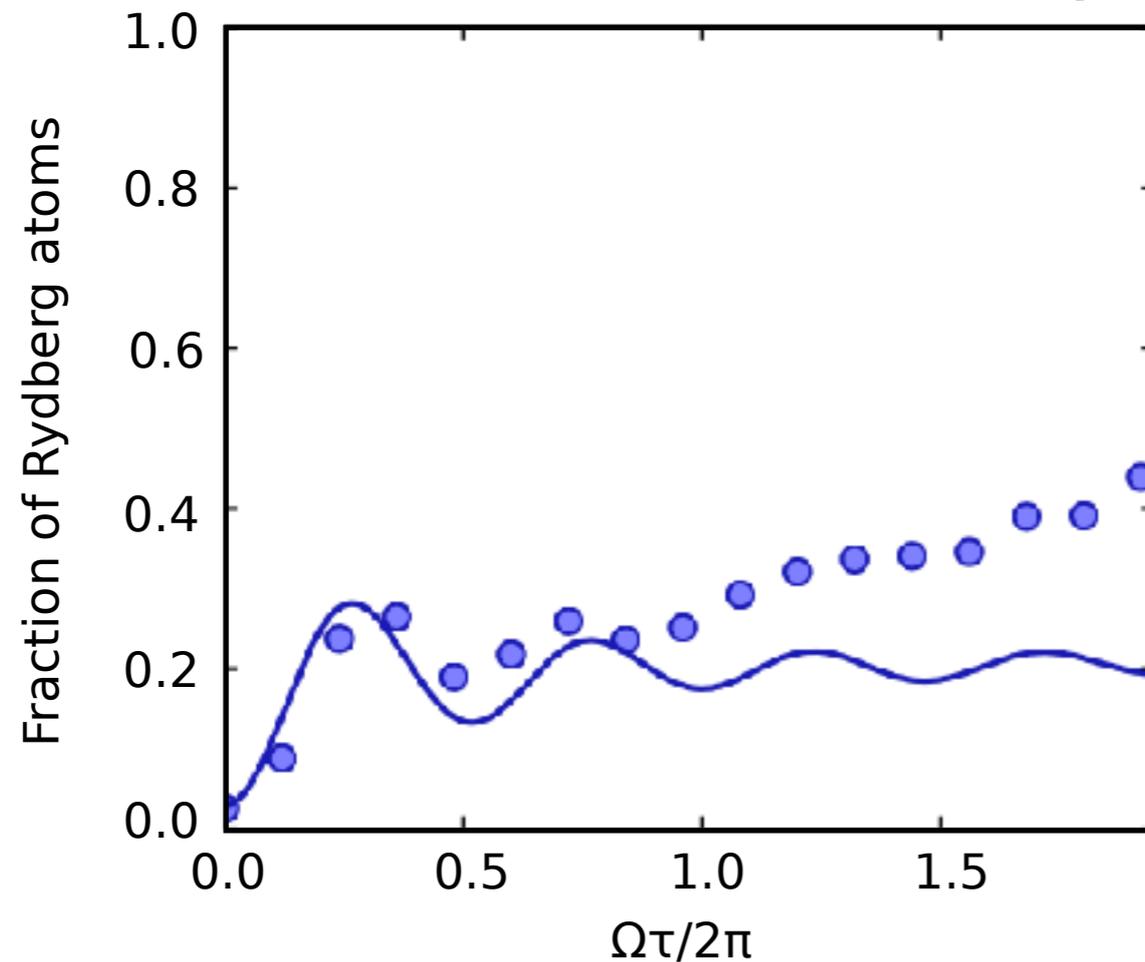


Quantum simulation of a defect-free 7x7 lattice

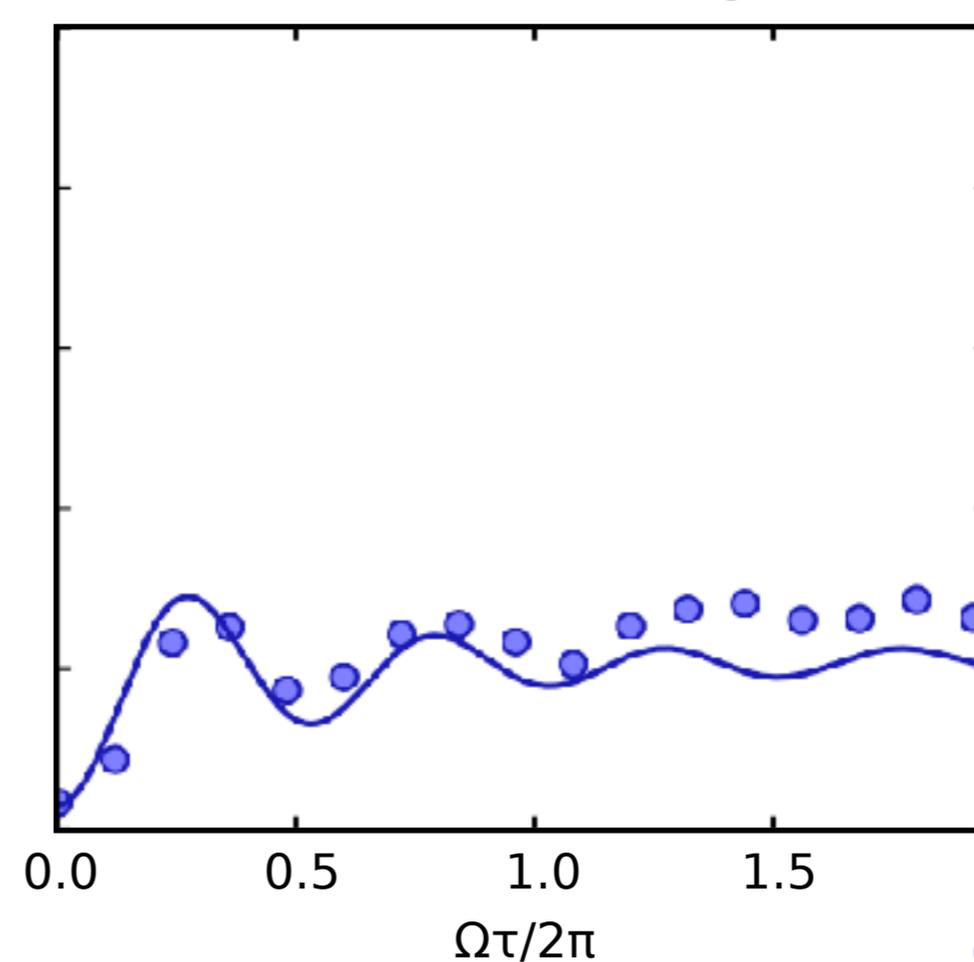


Prior to the experiment, stray electric field compensated better than 5 mV/cm

B = 6.9 G (E-field sensitivity)



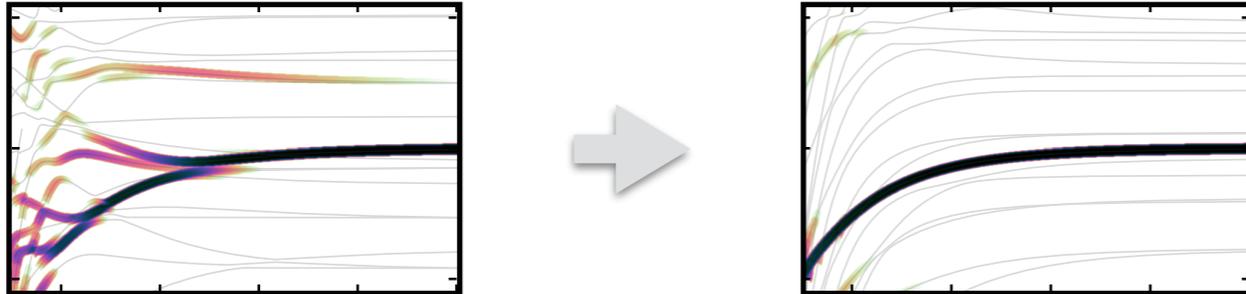
B = 3.5 G (ideal regime)



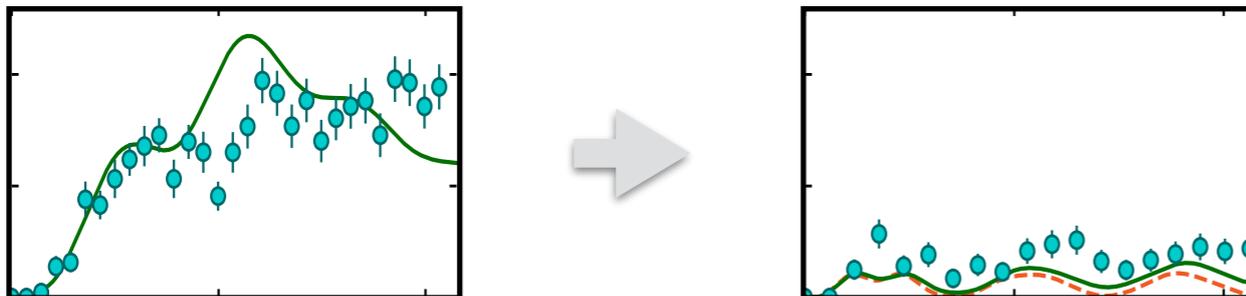
●● Experiment
— Spin-1/2 model

Conclusion

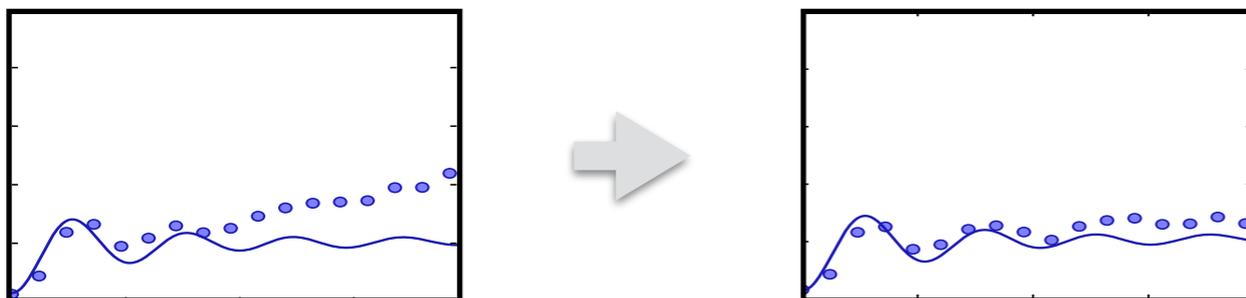
- E-field sensitivity of Rydberg blockade for D states, resolved by tuning the B-field



- Predictions verified in 2-atom blockade experiments

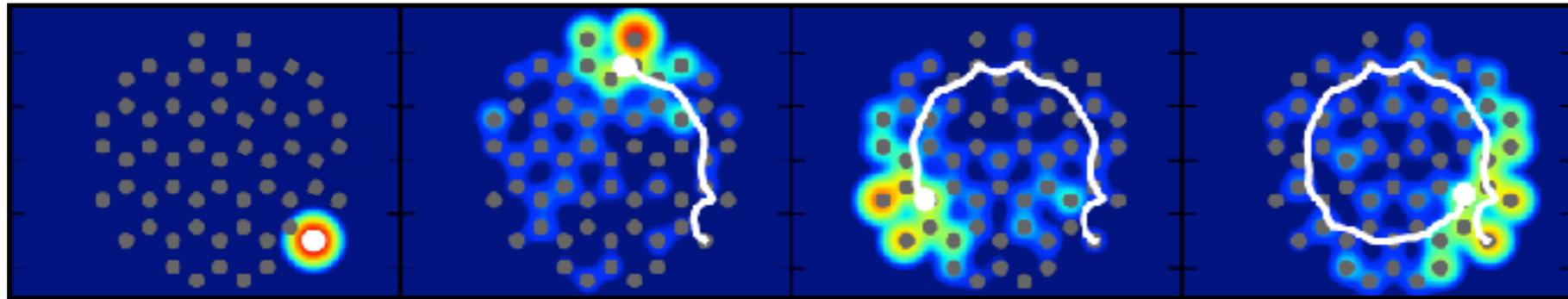


- Increased accuracy of Rydberg quantum simulations



Outlook

- Optimize further parameters
- Use optimization procedure for other experiments
- Investigate mapping to dipolar interacting spin-1 particles, e.g. useful for realizing topological bands



Details on ...

- pair potential calculations: J. Phys. B **50**, 133001 (2017)
- optimization of mapping to spin-1/2 particle: arXiv:1710.06156 (2017)